

# quantum field theory - course schedule

## Homework - grading

Homeworks, a take-home mid-term, and a final exam; the grades will be based on these (60%/20%/20%). Exams and homeworks include optional problems ("bonus" = extra credit). Homework assignments will be posted on the web every Thursday, due Tuesday, and by graded by your fellow students by the next Tuesday.

August 21

## 1. Lattice Field Theory

Diffusion as a sum over Paths

**Reading: [Chapter 1 - Lattice Field Theory](#)**

Cvitanović lecture notes

**Reading: [A. Zee Chapter I.1 - Who Needs It?](#)**

From A. Zee "Quantum Field Theory in a Nutshell"

**Reading: [C. Itzykson and J.-M. Drouffe - Statistical field theory, vol 1 \(Cambridge U. Press, 1991\)](#)**

Chapter 1: From Brownian motion to Euclidean fields (A nice discussion of free propagation as Brownian walks)

August 23

## 2. Discrete Fourier transforms

Fourier modes as eigenmodes of translation

**Reading: [Chapter 1 - Lattice Field Theory](#)**

Cvitanović lecture notes

**Homework #1 - problems**

- due Tue Aug 28, in class

August 28

## 3. Green's function in Quantum Mechanics

**Reading: [Chapter 2 - Path integral formulation of Quantum Mechanics](#)**

Cvitanović lecture notes

**Reading: [L.P. Kadanoff - Statistical Physics; Statics, Dynamics and Renormalization](#)**

Chapter 3: Gaussian Distributions (available online)

**Reading: [Physics Today - review](#)**

August 30

## 4. Path integral - Quantum Mechanics

**Reading: [A. Zee Chapter 2 - Path integral formulation of Quantum Mechanics](#)**

**Homework #2 - problems**

- due Tue Sep 4, in class

September 3

## Labor Day

September 4

## 5. Dirac-Feynman's Formulation of Quantum Mechanics

QM amplitudes as a sum over paths

**Reading: [Chapter 3 - Path integral formulation of Quantum Mechanics](#)**

Cvitanović lecture notes

**Reading: [Chapter 6 - Path Integrals in Quantum Mechanics](#)**

M. Srednicki book

September 6

## 6. Collective excitations

Elastodynamic equilibria of 1- and 2-dimensional solids. Phonons.

**Reading: A. Zee Chapter I.3 - From Mattress to Field**

**Reading: Section 1.6 - Collective excitations: from particles to fields**

Cvitanović lecture notes

**Homework #0 - template**

If you like to write up your solutions in LaTeX, here is a template

**Homework #3 - problems**

- due Tue Sep 11, in class

September 11

## 7. Qeefithe

**Reading: Fable - Qeefithe**

**Reading: Chapter 2 - Generating functionals**

What the mole saw

September 13

## 8. Qeefithe

Dyson-Schwinger equations

**Reading: Chapter 2 - Connected, 1PI Green's functions**

Tying the Nudo del Diablo

**Homework #4 - problems**

- due Tue Sep 18, in class

September 18

## 9. Qeefithe

**Reading: Chapter 3 - Path Integrals**

What the crow saw

September 20

## 10. Qeefithe

What the fox saw: it's just a Fourier transform. Tree expansions: Saddle point evaluation of path integrals, one loop (leading  $\hbar$ -bar) corrections. Ward identities: symmetries relate and constrain different Green's functions.

**Reading: Review - by Feynman**

**Reading: Chapter 5 - Field theory path integrals**

Cvitanović lecture notes

**Homework #5 - problems**

- due Tue Sep 25, in class

September 25

## 11. Perturbation expansions are asymptotic

Formally, perturbation series is always asymptotic, but can be very accurate.

**Reading: Section 5.6 - Saddle-point expansions are asymptotic**

Cvitanović lecture notes

**Reading: QED - is it finite, not asymptotic?**

September 27

## 12. Scalar field theory

The first physical result: Yukawa interaction by scalar fields (mesons) is attractive.

**Reading: A. Zee Chapter I.3 - From Mattress to Field**

**Reading: A. Zee Chapter I.4 - From Field to Particle to Force**

**Homework #6 - problems**

- due Thu Oct 11, in class

October 2

## 13. Scalar field theory

**Reading: A. Zee Chapter I.5 - Coulomb and Newton: Repulsion and Attraction**

**Reading: A. Zee Chapter I.11 - Field Theory Redux**

October 4

## 14. Effective action

While the full partition function for bare particle interactions is the easiest to derive, the physical content of a theory is given by the 'effective action', the interactions between dressed particles (this is a continuation of lecture 9, a deeper dive).

**Reading: Sections 2.H and 2.I - 1PI Green's functions, vacuum bubbles**

The 1pI generating functional is the Lagrange transform of the connected diagrams generating functional.

**Reading: Sections 3.E and 3.H - Legendre transforms**

The 1pI generating functional can be interpreted as the 'effective' (or 'quantum') action functional.

**Homework #7 - problems**

- due Thu Oct 18, in class

October 8-9

**fall recess**

October 11

**15. The Dirac Equation**

**Reading: A. Zee Chapter II.1 - The Dirac Equation**

**Reading: W. Greiner and J. Reinhardt - Dirac equation**

The excerpt in ChaosBook.org/library (click on Field Theory link) covers Dirac's original derivation of his equation.

October 16

**16. Midterm**

All material covered in the 1. part of the course, up to fall recess: generating functions, path integrals, their perturbative expansions, scalar fields propagators.

**Homework - midterm**

- usual time, in class

midterm grades distribution [all solutions are in the book]

October 18

**17. SU(2) and SO(3)**

Spin 1/2 is hiding in our Euclidean 3D space in plain sight, and nature has chosen to us it. Its representation theory will carry over also to the Minkowsky spacetime  $SO(1,3)$ .

**Reading: Notes 11.1 - SU(2) and SO(3)**

SU(2) - SO(3) correspondence

**Reading: W.G. Harter - Hamilton's turns**

(for fun only) How Hamilton (who would have guessed...) used quaternions to to extend the discrete Fourier transform from a circle to a sphere.

**Homework #8 - problems**

- due Thu Oct 25, in class

October 23

**18. SO(1,3) and SU(2) x SU(2)**

**Reading: Roger Penrose - Dirac's electron and antiparticles**

From "The Road to Reality". Skim through Chapt 24, read at least starting with section 24.7 The Dirac equation.

**Reading: Roger Penrose - The standard model of particle physics**

From "The Road to Reality". Skim through Chapt 25 at your pleasure, none of this will be on the final exam :)

**Reading: Jakob Schwichtenberg - SO(1,3) and SU(2) x SU(2)**

Refresh your OM, sect. 3.6 SU(2). Then work through the commutators of sect. 3.7 The Lorentz Group  $SO(1,3)$ . Make sure you know the distinction between Weyl, Majorana and Dirac spinors. Can skip sects. 3.7.11 Infinite-Dimensional Representations and 3.8 The Poincare Group, but do read sect. 3.9 Elementary Particles in preparation for learning about the Standard Model.

October 25 [lecturer: B.F.L. Ward](#)

**19. Celebrating 50 years of the Standard Model**

The role of Quantum Field Theory loop corrections in establishing the validity of the Standard Model (which David Gross now wants us to call the Standard Theory, in view of its experimental validation).

**Reading: Sabine Hossenfelder - String theory**

So you want to be a string theorist? Here are pros and cons.

**Homework #9 - problems**

- due Tue Nov 6, in class

October 30

## 20. gamma mu nu gymnastics

### Reading: V. K. - Dirac Matrices and Lorentz Spinors

The signature of the Minkowsky metric makes Lorentz transformations not unitary, and thus (complex conjugate transpose spinor)  $\times$  (complex spinor) is not a scalar under Lorentz transformations

### Reading: V. K. - Propagator for the Dirac Spinor Field

is perhaps what you would expect it to be

### Reading: Chapter 3 - Dirac equation

From Peskin and Schroeder, "An Introduction to Quantum Field Theory"; study pp. 35-44, 49-52, 62-63, rest we'll skip.

November 1

## 21. Feynman rules

### Reading: A. Zee Appendices C and D - Feynman rules

### Homework #10 - problems

- due Thu Nov 8

November 6 [lecturer: Brian Swingle](#)

## 22. How to calculate a signature of chaos in field theory using diagrams

This material ties into Swingle's 11:15am Theoretical Physics Seminar. Go hear it :)

### Reading: Debanjan Chowdhury and Brian Swingle - Onset of many-body chaos in the $O(N)$ model

The growth of commutators of initially commuting local operators diagnoses the onset of chaos in quantum many-body systems.

November 8

## 23. Feynman rules

### Reading: P. Cvitanovic - Feynman rules part I

Apologies for bad audio - this was the first test of recording online lectures. Mouse over video's top edge to change the resolution.

### Reading: P. Cvitanovic - Feynman rules part II

Big day: our first QED Feynman integral. Click on video's gearwheel, lower right edge, to change the resolution.

### Homework #11 - problems

- due Thu Nov 13, in class

November 13

## 24. Electron magnetic moment

### Reading: A. Zee Chapter VIII.3 - The treshold of ignorance

### Reading: A. Zee Chapter III.4-6 - Electron magnetic moment

Skim through Chapt III.4-5, work through Chapt III.6 Sect "Dirac's triumph".

### Reading: P. Cvitanovic - Electron magnetic moment (Dirac triumph) (part 1)

Big day: our first QED Feynman integral. Click on video's gearwheel, lower right edge, to change the resolution.

### Reading: P. Cvitanovic - Electron magnetic moment (Dirac triumph) (part 2)

Dirac explains a factor of 2 in observed electron magnetic moment.

### Reading: P. Cvitanovic - Electron magnetic moment (Dirac triumph) (part 3)

Schwinger's vertex.

November 15

## 25. Feynman Diagrams

### Reading: D. Kaiser - Physics and Feynman's Diagrams

American Scientist 93, 156 (2005)

### Reading: Kelly Devine Thomas - Feynman Diagrams and the Evolution of Particle Physics

The Institute Letter, I.A.S. (Spring 2009)

### Reading: P. Cvitanovic - a very brief history of diagrammatics

(worth a glance) A lightning fast way to compute commutators, but you have to learn how to draw first. See page 38.

### Reading: L. Dixon - Look ma - no Feynman's diagrams!

How we calculate amplitudes these days (October 3, 2013)

### Homework #12 - problems

- due Tue Nov 20, in class

November 15; recorded July 25, 2013 [lecturer: Edward Witten](#)

## 25 extra Feynman Diagrams in String Theory

**Reading: video - What any physicist should know**

even if she does not want to do mess with strings.

**Reading: Freeman J. Dyson - The World on a String**

To balance the pied piper song - a delightful sceptic's view.

November 20 [lecturer: Ignacio Taboada](#)

## 26. Standard Model

**Reading: Apostolos Vasileiadis - Symmetry**

(for fun only) Gauge invariance is not preserved!

**Homework - no problem**

- none due this week

November 21-23

## Thanksgiving

November 27

## 27. Electron magnetic moment

**Reading: A. Zee Chapter III.6 - Electron magnetic moment**

Work through Chapt III.6 Sect "Schwinger's triumph".

**Reading: Matthew Schwartz Chapter III-3: - The anomalous magnetic moment**

Complementary, even more compact than Zee's derivation.

**Reading: Appendices C and D - Feynman rules**

Referred to in calculations of Chapt III.6.

**Reading: P. Cvitanovic - Anomalous electron magnetic moment (Schwinger's triumph)**

Schwinger's  $\alpha/2\pi$  calculation sketched out. (You'll have to screw up the volume, sorry.)

**Reading: Dan Styer - Calculation of the anomalous magnetic moment of the electron**

The accuracy available as of 21 June 2012 "is the equivalent of measuring the distance from Los Angeles to New York to within the width of a bacterium, or of measuring the distance from the Earth to the Moon to within the width of a single human hair."

**Reading: Toichiro Kinoshita - Fine Structure Constant, Electron Anomalous Magnetic Moment, and Quantum Electrodynamics**

The heroic calculation of Toichiro Kinoshita: status as of 2010.

[Schwinger's headstone]

November 29

## 28. Gauge invariance

Ward identities: symmetries relate and constrain different Green's functions.

**Reading: Sections 3.G and 3.H - Point transformations**

**Reading: A. Zee Chapter III.4 - Gauge invariance: A photon can find no rest**

**Reading: Sections 3.A and 3.B - Ghoulies and ghosties**

**Reading: A. Shapere and F. Wilczek - Geometry of self-propulsion at low Reynolds number**

(Not covered in this lecture, but might interest you:) From swimming to gauge potentials. But what is a photon, really?

**Reading: The base space (space of unlocated shapes) - for cats**

A fibration and a base space :)

**Homework #13 - problems**

- due Tue Dec 4, in class

December 4

## 29. Renormalization

**Reading: Chapter \* - Parametric representation**

Unpublished notes: momentum space Feynman integrals, parametric representation.

**Reading: Chapter \* - Renormalization**

Unpublished notes: Power counting, UV divergences, subtractions, counterterms.

**Reading: Chapter \* - Gauge-invariant sets**

Unpublished notes: high-orders diseases; gauge set counting; finiteness conjecture.

December 4

## GT classes end

### **Homework Final exam - syllabus**

An overview of material covered by the final exam.

[midterm grades]

December 6 - freebie

## 30. Gribov copies

**Reading: Higgs Boson - blues**

**Reading: Nick Cave - and The Bad Seeds**

The full length version

December 10

## final exam 2:40pm - 5:30pm

closed book, closed lecture notes.

Course grades distribution [alert me if I am missing some homework grades]

until December ?

## course opinion survey

CETL web link

October 29 - December 14

## spring registration

**Reading: PHYS-7143 - Group Theory**

The Spring 2019 group theory course can be described this way: Suppose someone came to you and asked, "On planet Z, mesons consist of quarks and antiquarks, but baryons contain three quarks in a symmetric color combination. What is the symmetry group?" The answer requires some thought, and leads to magic that bequiles field theorists. We might get to the answer by the end of the course - but our focus will be on basic tools of group theory: finite groups, subgroups, cosets, and conjugacy, group of permutations, matrix representations, tensors, Schur's Lemma, characters and character table construction, irreducible representations, Lie groups, rotations and why you need no Clebsch-Gordon coefficients. Hope you will join me. Tell your friends to join us too.

December 17

## GT grades due at noon

December 24

## the future looks bright

Future's So Bright, I Gotta Wear Shades [click right, open in new tab]

svn: \$Author: predrag \$ - \$Date: 2018-12-01 20:44:03 -0500 (Sat, 01 Dec 2018) \$